CALCULUS 30: OUTCOME 4B DAY 1 – THE POWER RULE & SUM/DIFFERENCE RULE

### To learn and apply the power rule and the sum and difference rules for differentiation..

### VIDEO LINKS: a) <u>https://goo.gl/FBSgsy</u>

c) <u>https://goo.gl/rx6FpV</u>

Do you see any patterns in the following questions between f(x) and the FINAL answer for f'(x)? Can we use this pattern to jump right to the answer without doing any of the "limit" work in between?

If  $f(x) = 3x^2$ , find f'(x)  $f'(x) = \lim_{h \to 0} \frac{[3(x+h)^2] - [3x^2]}{h}$   $f'(x) = \lim_{h \to 0} \frac{[3x^2 + 6xh + 3h^2] - [3x^2]}{h}$   $f'(x) = \lim_{h \to 0} \frac{[3x^2 + 6xh + 3h^2] - [3x^2]}{h}$   $f'(x) = \lim_{h \to 0} \frac{[3x^2 + 6xh + 3h^2] - [3x^2]}{h}$   $f'(x) = \lim_{h \to 0} \frac{3h^2 + 6xh}{h}$   $f'(x) = \lim_{h \to 0} \frac{3h^2 + 6xh}{h}$   $f'(x) = \lim_{h \to 0} \frac{3h^2 + 6xh}{h}$  $f'(x) = \lim_{h \to 0} \frac{3h + 6x}{h}$ 

If 
$$f(x) = 5x^3$$
, find  $f'(x)$   
 $f'(x) = \lim_{h \to 0} \frac{\left[5(x+h)^3\right] - \left[5x^3\right]}{h}$   
 $f'(x) = \lim_{h \to 0} \frac{\left[5x^3 + 15x^2h + 15xh^2 + 5h^3\right] - \left[5x^3\right]}{h}$   
 $f'(x) = \lim_{h \to 0} \frac{15x^2h + 15xh^2 + 5h^3}{h}$   
 $f'(x) = \lim_{h \to 0} \frac{h(15x^2 + 15xh + 5h^2)}{h}$   
 $f'(x) = \lim_{h \to 0} 15x^2 + 15xh + 5h^2$   
 $f'(x) = 15x^2$ 

• So far, we have been using  $\lim_{h \to 0} \frac{f(x+h) - f(x)}{h}$  to find the slope of the tangent line of the curve y = f(x) at the dy

general point (x, f(x)), also called the derivative, or f'(x) or  $\frac{dy}{dx}$ .

• This takes a lot of time and mistakes can be easily made if you are not careful. There is an easier way!!

### **DERIVATIVES :** Do you notice the pattern in the following examples?

a) 
$$s(t) = 3t$$
  
 $s^{(t)} = 3$ 
b)  $f(x) = 7x^{2}$   
 $f^{(x)} = 14x$ 
c)  $f(x) = -9x^{5}$   
 $f^{(x)} = -45x^{4}$ 
d)  $f(x) = \frac{10}{x}$   
 $f(x) = 10x^{-1}$   
 $f^{(x)} = -10x^{-2}$ 

### THE POWER RULE (part 1):

- If  $f(x) = x^n$ , where n is a real number, then  $f'(x) = nx^{n-1}$
- In Leibniz notation we say that  $\frac{d}{dx}x^n = nx^{n-1}$ .

### THE POWER RULE (part 2):

- If  $f(x) = cx^n$ , where c is a constant and n is a real number, then  $f'(x) = (c)(n)x^{n-1}$
- In Leibniz notation we say that  $\frac{d}{dx} [cf(x)] = c \frac{d}{dx} f(x)$

**Ex #1:** Find f(x) or  $\frac{dy}{dx}$  of the following functions:

a) 
$$f(x) = x^{15}$$
 b)  $f(x) = \frac{1}{x^3}$  c)  $f(x) = \sqrt{x}$  d)  $f(x) = \frac{1}{\sqrt[3]{x^2}}$ 

<u>NOTE</u>: At this point we often negative exponents in the answers. We will sometimes leave radicals in the denominator and not rationalize the denominator.

**Ex #2:** Find 
$$f(x)$$
 or  $\frac{dy}{dx}$  of the following functions:  
a)  $f(x) = -4x^{15}$  b)  $f(x) = (5x^4)^3$  c)  $f(x) = \sqrt{7x}$ 

d) 
$$f(x) = \sqrt[3]{\frac{4}{x^2}}$$

**THE CONSTANT RULE:** If f(x) = c, where c is a constant (#), then f'(x) = 0 (Proof on P 78)

**Ex #3:** If f(x) = -5, determine f'(x).

**Ex #4:** Find the equation of the tangent line to the curve  $y = x^5$  at the point (2,32).

### THE SUM/DIFFERENCE RULE:

If f(x) is the sum of 2 differentiable functions  $f(x) = g(x) \pm h(x)$  ) then  $f'(x) = g'(x) \pm h'(x)$ 

**Ex #5:** Find f'(x) or  $\frac{dy}{dx}$  of the following functions: a)  $f(x) = 2x^3 + 7x^6$  b)  $f(x) = (4x-3)^2$ 

c) $f(x) = \frac{\pi x^6}{2} + x - \frac{3}{x}$	d) $f(x) = \frac{(3x-5)(3x+5)}{x^5}$
c) $f(x) = \frac{-1}{2} + x - \frac{-1}{x}$	d) $f(x) = \frac{x^5}{x^5}$

**Ex #6:** At what point on the curve  $y = -x^2 + 3x + 4$  does the tangent line have a slope of 5?

**Ex #4:** A ball is dropped from the upper observation deck of the CN Tower. The distance fallen, in metres, after *t* seconds is  $s = 4.9t^2$ . How fast is the ball falling after 3 seconds?

### OUTCOME 4B DAY 1 ASSIGNMENT (Section 2.2 & 2.3 in Text)

FATEXTBOOK P83 #1, 2a-k, 3ace, 4bandP88 1a-j, 3ab, 2ac, 4MLATEXTBOOK P83 # 2lmn, 4cd, 7, 8andP88 #1kl, 2bd, 3acd, 5, 6, 7

CALCULUS 30: OUTCOME 4B DAY 2 – THE PRODUCT RULE (SECTION 2.4)

### To learn and apply the PRODUCT rule for differentiation..

VIDEO LINKS: a) <u>https://goo.gl/dpwnaL</u> b) <u>https://goo.gl/ArF6WU</u>

### THE PRODUCT RULE:

• When you are taking the derivative of the product of two expressions, the derivative will be

$$[f(x)g(x)]' = f(x)g'(x) + g(x)f'(x)$$

In other words, the derivative of the product of two expressions will be:

(first expression)(derivative of second expression) + (second expression)(derivative of first expression)

We can also reword th

NOTE: It's very important to realize that the derivative of a product DOES NOT equal the product of the derivatives  $[f(x)g(x)]' \neq f'(x)g'(x)$ 

**Ex #1:** Find the derivative,  $\frac{dy}{dx}$  if  $y = (2x^3 + 7)(3x^2 - x)$ . Use the product law.

**Ex #2:** Differentiate  $f(x) = \sqrt{x(2-3x)}$  using the product law and simplify. Express your answer using a common denominator.

**Ex #3:** Find the equation of the tangent line to the graph of  $f(x) = (3x^2 + 2)(2x^3 - 1)$  when x = 1.

**Ex #4:** Find the slope of  $y = \left(4\sqrt{x} + \frac{2}{x^2}\right)\left(\sqrt[3]{x} - x^3\right)$  at the point x = 1

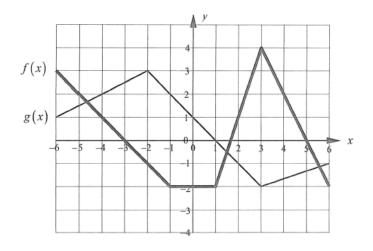
### OUTCOME 4B DAY 2 ASSIGNMENT (Section 2.4 in Text)

### FA TEXTBOOK P 92 #1, 2abdeh, 3, 5

MLA TEXTBOOK P92 #6 Plus the following:

Shown at right is a graph of the functions f(x) and g(x). Assume that  $F(x) = f(x) \cdot g(x)$ . By studying the graph and using the product rule, determine the value of each of the following. 21. F'(2)22. F'(-4)

- 23. F'(0)
- 24. F'(3)
- 25. If  $f(x) = (x^2 + 3x)^5$ , use the product rule to show that  $f'(x) = 5(x^2 + 3x)^4(2x + 3)$ .



CALCULUS 30: OUTCOME 4B DAY 3 – THE QUOTIENT RULE (SECTION 2.5)

### To learn and apply the QUOTIENT rule for differentiation..

VIDEO LINKS: a) <u>https://goo.gl/yxPB3X</u>

b) <u>https://goo.gl/QEbwCz</u>

### THE QUOTIENT RULE:

• Given a function in the form of a quotient,  $F(x) = \frac{f(x)}{g(x)}$ , then  $F'(x) = \frac{g(x)f'(x) - f(x)g'(x)}{\left\lceil g(x) \right\rceil^2}$ .

(Note that we are using a capital F(x) for the quotient function)

- In other words, the derivative of the product of two expressions will be: [(bottom)(derivative of top) – (top)(derivative of bottom)] divided by (bottom squared)
- It is customary NOT to expand the expression in the denominator when applying the quotient rule

**Ex #1:** Differentiate  $F(x) = \frac{x^2 + 2x - 3}{x^3 - 1}$ .

**Ex #2:** Find 
$$\frac{dy}{dx}$$
 if  $y = \frac{\sqrt{x}}{1+2x}$ .

**Ex #3:** Find the equation of the tangent line to the curve  $f(x) = \frac{\sqrt{x}}{x+2}$  at the point (4, -1). Express your answers in GENERAL FORM (Ax + By + C = 0).

**Ex #4:** Find the coordinates of two points on the graph of the function  $f(x) = \frac{10x}{x^2 + 1}$  at which the tangent line is horizontal.

### OUTCOME 4B DAY 3 ASSIGNMENT (Section 2.5 in Text)

#### **TEXTBOOK P** 95 #1a-I, 2, 3abc, 6 FA

MLA TEXTBOOK P 95 #2, 5, 7, 8 Plus the following (Please remember that MLA questions could be found on the test!) Some ice cubes were added to a cup of boiling water. The temperature of the water in degrees Celsius t minutes after the ice cubes were added, can be approximated by the function		
	$T(t) = \frac{20t^2 + 100t + 200}{t^2 + t + 2}$ . Round your answers to two decimal places where necessary.	
	(a) Find $T(0)$ , $T(1)$ , and $T(5)$ . Interpret your answers.	
	(b) Find $T'(t)$ .	
(c) Find $T'(1)$ and $T'(5)$ . Interpret your answers.		
(d) Find $\lim_{t \to \infty} \frac{20t^2 + 100t + 200}{t^2 + t + 2}$ and interpret your result.		
Calculus 30(Ms. Carig	(nan) C30.4B Differentiation Rules	P <b>age 9</b>

**CALCULUS 30:** OUTCOME 4B DAY 4 – THE CHAIN RULE (SECTION 2.6)

### To learn and apply the CHAIN rule for differentiation.

VIDEO LINKS: a) <u>https://goo.gl/8rSQrd</u> b) <u>https://goo.gl/cQ9jEG</u> c) <u>https://goo.gl/cJnw2Z</u>

### THE CHAIN RULE:

• When we have a function within a function, we need an additional rule called the CHAIN RULE. The chain rule must be used when we have a function whose derivative is not 1 within another function such as a power, a root, or a combination of those. Here are some examples of functions within functions (composite functions)

 $y = (5x-4)^{6}$   $y = 7(x^{5}-4)^{7}$   $y = \sqrt{(7x^{5}-8x+2)^{3}}$ 

We often rewrite the function by rewriting the function using a substitution of *u* for the "inner" function

let $u = 5x - 4$	let $u = x^5 - 4$	$let u = \left(7x^5 - 8x + 2\right)$
$y = (u)^6$	$y = 7(u)^7$	$y = \sqrt{u^3}$

• Once we have made the substitution, we take the derivative using the chain rule. Typically, our

functions contain x and y variables, so we usually find the derivative of y with respect to x, as in  $\frac{dy}{dx}$ .

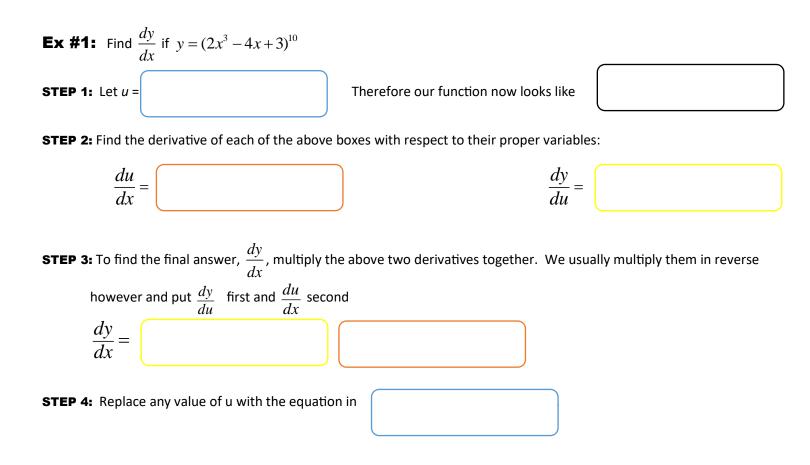
As we have changed the variable from x to u in the above questions, we need to adapt the formula to now take the derivative of y with respect to u while taking into account that u is based on a foundatior of the x variable. The chain rule will produce the following:

$$\frac{dy}{dx} = \frac{dy}{du} \cdot \frac{du}{dx}$$

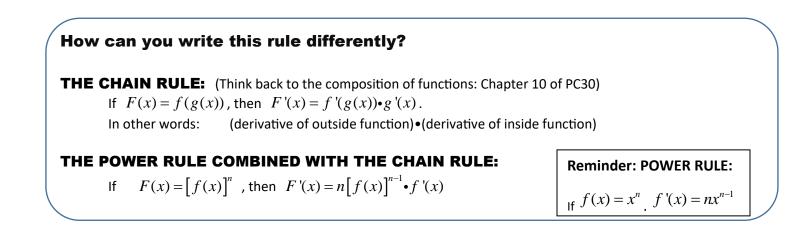
- This means: To find the derivative of the original function y, with respect to the original function in terms of x, you need to
  - 1) Find the derivative of the newly rewritten function *y* (containing the *u*) with
    - respect to the variable *u*. This is the  $\frac{dy}{du}$  part of  $\frac{dy}{dx} = \frac{dy}{du} \cdot \frac{du}{dx}$
  - 2) Multiply your answer in step 1 by the derivative of the equation u with

respect to the variable x. This is the 
$$\frac{du}{dx}$$
 part of  $\frac{dy}{dx} = \frac{dy}{du} \cdot \frac{du}{dx}$ 

3) You now need to go back and replace any remaining *u* values with the equation that it represents in terms of *x*. We will often leave this answer fairly unsimplified and it may often contain negative or rational exponents.



**STEP 5:** Simplify where appropriate. Combine like terms or expressions/ factor and reduce etc.



**Ex #2:** Differentiate  $y = \sqrt[3]{(2x^5 - 1)^2}$ 

b) 
$$f(x) = \frac{1}{\sqrt[3]{1-x^4}}$$

**Ex #3:** If 
$$y = u^{10} + u^5 + 2$$
 where  $u = 1 - 3x^2$ , find  $\frac{dy}{dx}\Big]_{x=1}$  by first using  $\frac{dy}{dx} = \frac{dy}{du}\frac{du}{dx}$ .

Now, when x = 1, u =

So, 
$$\frac{dy}{dx} \bigg|_{x=1} =$$

OUTCOME 4B DAY 4 ASSIGNMENT (Section 2.6 in Text)

FA TEXTBOOK P 102 #1a-h, 3, 4, 7 MLA TEXTBOOK P102 #5, 9 CALCULUS 30: OUTCOME 4B DAY 5 – THE CHAIN RULE CONT. (SECTION 2.6)

To combine the chain rule with all other rules for differentiation (power, sum, difference, product, quotient).

VIDEO LINKS: a) <u>https://goo.gl/qhufnM</u>

b) https://goo.gl/rjoMJo

**Ex #1:** Differentiate: a)  $y = (x^2 + 1)^3 (2 - 3x)^4$ 

b) 
$$s(t) = \left(\frac{2t-1}{t+2}\right)^6$$

c) 
$$F(x) = \sqrt{x + \sqrt{x^2 + 1}}$$

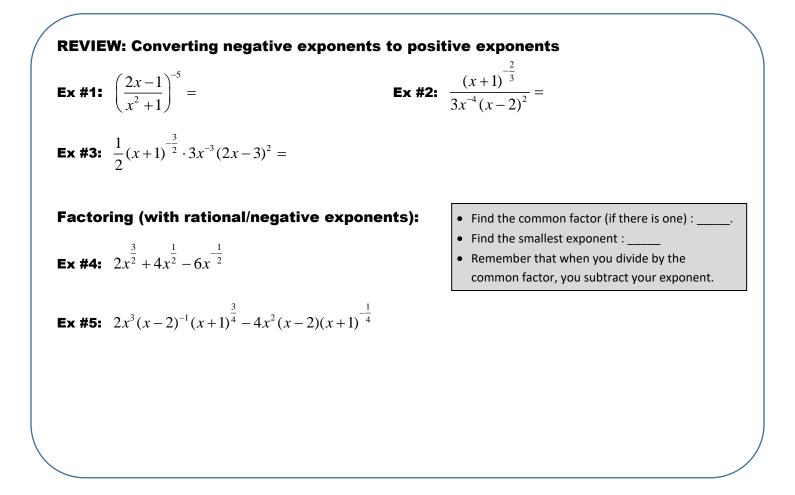
## OUTCOME 4 DAY 12 ASSIGNMENT (Section 2.6 in Text): p.102 #1i-I, 6acegil

FA TEXTBOOK P 102 #1i-l, 6acegil MLA TEXTBOOK P102 #5, 9

### **CALCULUS 30:** OUTCOME 4B DAY 6 – COMBINING RULES (SIMPLIFIED ANSWERS)

VIDEO LINKS: a) <u>https://goo.gl/t98bBj</u>

b) <u>https://goo.gl/rjoMJo</u>



**Ex #1:** Certain functions can be solved using different methods. To find the derivative of the following functions, what rules could you use? Choose the easiest option and differentiate the functions.

a) 
$$y = \frac{3}{\sqrt{(x-2)^3}}$$
 b)  $f(x) = \frac{x(x^2+3)}{(x-2)^4}$ 

Find the derivative of each of the following functions, writing your answers in factored form where possible.

1. 
$$f(x) = 2x^3 + 15x^2 - 36x + 12$$
  
2.  $f(x) = -2x^{-3} - \frac{1}{2}x^{-2} + x^{-1} + 11$   
3.  $y = \frac{1}{x} + 4x$   
5.  $f(x) = (2x-3)^3 (x+1)^2$   
7.  $y = (x-2)\sqrt{x^2 - 3x - 1}$   
9.  $f(x) = \frac{x^2 - 3x}{x^2 + 3}$   
11.  $y = x^3 (2x-1)(3x+2)$   
13.  $f(x) = (\frac{2x}{x+2})^{-2}$   
15.  $y = \frac{\sqrt{x}}{x^2 + 1}$   
17.  $f(x) = \frac{1}{(x^2 - 2)\sqrt{2x + 3}}$   
2.  $f(x) = -2x^{-3} - \frac{1}{2}x^{-2} + x^{-1} + 11$   
4.  $y = \sqrt{x} + \frac{5}{\sqrt{x}} - \frac{x}{\sqrt{5}}$   
6.  $f(x) = x^2\sqrt{1 - x^2}$   
7.  $y = (x-2)\sqrt{x^2 - 3x - 1}$   
10.  $f(x) = \frac{6}{\sqrt[3]{x^3 - 2}}$   
11.  $y = x^3 (2x-1)(3x+2)$   
12.  $y = \frac{x(2x-3)}{x^2 + 2}$   
14.  $f(x) = \frac{(x+1)^2}{x^2 - 2}$   
15.  $y = \frac{\sqrt{x}}{x^2 + 1}$   
16.  $f(x) = \sqrt{\frac{3 - x}{x^4}}$   
17.  $f(x) = \frac{1}{(x^2 - 2)\sqrt{2x + 3}}$   
18.  $f(x) = \sqrt{\frac{x+4}{x-4}}$ 

**CALCULUS 30:** OUTCOME 4B DAY 7 – IMPLICIT DIFFERENTIATION (SECTION 2.7)

### To learn and apply implicit differentiation versus explicit differentiation.

VIDEO LINKS: a) <u>https://goo.gl/8rSQrd</u> b) <u>https://goo.gl/cQ9jEG</u> c) <u>https://goo.gl/cJnw2Z</u>

• So far, our functions have been **explicitly defined**, which is when y is already isolated.

• Ex: 
$$y = x^5 + 3x - 1$$

- We will now be working with **implicitly defined** functions, where we cannot solve for y.
  - Ex:  $x^2 y^3 + 3xy = 1$

### **Review of Notations:**

 $\frac{d}{dx}(x^3)$  means: find the derivative of  $x^3$  with respect to x.  $\frac{d}{dx}(x^3) = \frac{d}{dx}(y^4)$  means: find the derivative of  $y^4$  with respect to x.  $\frac{d}{dx}(y^4) =$  This is challenging as there are no x's

• To take the derivative of a function that is defined implicity, we take the derivative from left to right, and wherever there is a value of y in the equation, we need to use the chain rule and multiply that

term by  $\frac{dy}{dx}$ . We normally use the chain rule when taking the derivative of x values but the chain rule

of those terms ends up being 
$$\frac{dx}{dx}$$
 which reduces to 1.

**Ex #1:** Find 
$$\frac{d}{dx}(12y^{-\frac{1}{3}})$$
.

**Ex #2:** Differentiate from left to right with respect to x :

a) 
$$\frac{d}{dx}(9x^2 - 4y^{-\frac{1}{4}})$$

b) 
$$\frac{d}{dx}(2x^3y^4)$$

# USING IMPLICIT DIFFERENTIATION when working with EQUATIONS containing a mixture of x and y:

**STEP 1:** Differentiate **both sides of the equation**, from left to right, **with respect to x**.

**STEP 2:** Collect all the terms with  $\frac{dy}{dx}$  on one side of the equation **STEP 3:** Factor out the  $\frac{dy}{dx}$ **STEP 4:** Isolate  $\frac{dy}{dx}$ .

Using implicit differentiation is easier than explicit differentiation. Here is an example as to why:

**Ex #2:** If  $x^2 + y^2 = 169$ , find  $\frac{dy}{dx}$  implicitly. Then, find the equation of the tangent line to this circle at (12,-5).

**Ex #3:** Suppose  $x^2y + 2y^2 - x = 3$ . Find  $\frac{dy}{dx}$ .

**Ex #4:** Find the slope and the equation of the tangent line (in standard form) to the curve  $x^3 - 3x^2y + y^2 = 3$  at (-1,4)

### OUTCOME 4B DAY 7 ASSIGNMENT : p.107 #1, 2a-d,f, 3, 5, 7(challenge)

FA TEXTBOOK P 107 #1, 2a-d, f, 3, 5a MLA TEXTBOOK P107 # 6, 7 CALCULUS 30: OUTCOME 4B DAY 8 – HIGHER ORDER DERIVATIVES (SECTION 2.8)

#### To learn and apply higher order derivatives.

VIDEO LINKS: a) <u>https://goo.gl/rAKqEw</u> b) <u>https://goo.gl/VGMa9o</u>

### Higher Order Derivatives:

- We can take the derivative of a derivative function, and the derivative of that function and so on.
- A first derivative is written as f'(x) or  $\frac{dy}{dx}$ 
  - A first derivative represents the slope of a tangent line or rate of change (how the slope of the original function changes). A common example of the first derivative is that velocity is a first derivative of a distance function.

• A second derivative is written as 
$$f''(x)$$
 or  $\frac{d^2y}{dx^2}$ 

 A second derivative measures how fast the first derivative function (often velocity) is changing, specifically how the rate of change/slope of the tangent line of the original function changes. A common example of the second derivative is acceleration in that acceleration is the second derivative of a distance function (but the first derivative of a velocity function)

• A third derivative is written as 
$$f''(x)$$
 or  $\frac{d^3y}{dx^3}$ 

- An example of a third derivative measures how fast acceleration is changing with respect to time. In physics this can also be known as jerk/jolt/surge or lurch.
- If a distance formula y = s(t), then

 $\circ$  If, however, the initial function y = v(t) then it's first derivative y' = a(t)

**Ex #1:** Find 
$$\frac{d^2 y}{dx^2}$$
 if  $y = x^6$ 

**Ex #2:** Find the second derivative of  $f(x) = 5x^2 + \sqrt{x}$ 

**Ex #3:** Find f''(1) if  $f(x) = (2 - x^2)^{10}$ 

**Ex #4:** If  $x^3 + y^3 = 5$ , use implicit differentiation to find  $\frac{d^2 y}{dx^2}$ .

OUTCOME 4B DAY 8 ASSIGNMENT :

FA TEXTBOOK P 111 #1odd, 2, 3, 4, 5 MLA TEXTBOOK P 111 #7, 8

### OUTCOME 4B REVIEW ASSIGNMENT

P 112 #4a-n, 5a, 7abc, 8, 9ade PLUS the following:

- 1. Find the coordinates of two points on the graph of  $f(x) = 4x^3 + x^2 + 2x + 8$  at which the slope of the tangent line is 4.
- 2. Find  $\frac{d^2 y}{dx^2}$  given the equation  $2y^2 xy = 6$

Solutions: 1.  $\left(-\frac{1}{2}, \frac{3}{4}\right)$  and  $\left(\frac{1}{3}, \frac{44}{27}\right)$  2.  $\frac{d^2y}{dx^2} = \frac{12}{\left(4y - x\right)^3}$ 

# **CALCULUS 30: SOLUTIONS TO WORKBOOK ASSIGNMENTS**

### **SOLUTIONS TO: OUTCOME 4B DAY 2 ASSIGNMENT**

### **EXTRA QUESTIONS:**

21. F'(2) = f'(2)g(2) + f(2)g'(2) = (3)(-1) + (1)(-1) = -4 22.  $-\frac{3}{2}$  23. 2 24. F'(3) does not exist since f'(3) and g'(3) do not exist. 25. Let  $g(x) = x^2 + 3x$ . Then g'(x) = 2x + 3. Now  $f(x) = (x^2 + 3x)^5 = \lfloor g(x) \rfloor^5 = \lfloor g(x) \rfloor \rfloor \lfloor g(x) \rfloor \rfloor \lfloor g(x) \rfloor \lfloor g(x) \rfloor \lfloor g(x) \rfloor \lfloor g(x) \rfloor \rfloor \lfloor g(x) \rfloor \rfloor$ 

### SOLUTIONS TO: OUTCOME 4B DAY 3 ASSIGNMENT

### **EXTRA QUESTIONS:**

. (a) 
$$T(0) = 100$$
,  $T(1) = 80$ ,  $T(5) = 37.5$ ;

initially the water was  $100^{\circ}C$ , after 1 minute it was  $80^{\circ}C$ , after 5 minutes it was  $37.5^{\circ}C$  (b)  $\frac{-80t^2 - 320t}{(t^2 + t + 2)^2}$ 

(c) T'(1) = -25, T'(5) = -3.52; after 1 minute the temperature is falling at a rate of  $25^{\circ}C/\min$  and

after 5 minutes the temperature is falling at a rate of  $3.52^{\circ}C/\min$ . (d) 20; As time passes the temperature of the water cools towards  $20^{\circ}C$ , likely the room temperature.

### **SOLUTIONS TO: OUTCOME 4B DAY 6 ASSIGNMENT**

1. 6(x-1)(x+6) 2.  $-x^{-4}(x-3)(x+2)$  3.  $x^{-2}(2x-1)(2x+1)$  4.  $\frac{1}{2\sqrt{5}}x^{-1/2} - \frac{5}{2}x^{-3/2} - \frac{1}{\sqrt{5}}$ 5.  $10x(x+1)(2x-3)^2$  6.  $-x(3x^2-2)(1-x^2)^{-1/2}$  7.  $\frac{1}{2}(4x^2-13x+4)(x^2-3x-1)^{-1/2}$ 8.  $2(x-1)^{-1/2} - 3(x+1)^{-1/2}$  9.  $\frac{3(x-1)(x+3)}{(x^2+3)^2}$  10.  $-6x^2(x^3-2)^{-4/3}$  11.  $2x^2(15x^2+2x-3)$ 12.  $\frac{3x^2+8x-6}{(x^2+2)^2}$  13.  $\frac{-(x+2)}{x^3}$  14.  $\frac{-2(x+1)(x+2)}{(x^2-2)^2}$  15.  $\frac{1-3x^2}{2x^{1/2}(x^2+1)^2}$  16.  $\frac{1}{2}x^{-5}(7x-24)(3-x)^{-1/2}$ 17.  $-(5x^2+6x-2)(x^2-2)^{-2}(2x+3)^{-3/2}$  18.  $-4(x+4)^{-1/2}(x-4)^{-3/2}$